

# Probability and Statistics

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Probability and Statistics: January 2017 - May 2017

## Large Sample Confidence Intervals

For a population mean and proportion:

	population distribution type	sample size	population standard deviation
Section 7.1	normal	any	known
Section 7.2	any	large	unknown

### Section 7.1

$$\bar{x} \pm z_{\alpha/2} \frac{\sigma}{\sqrt{n}}$$

is a large sample confidence interval for  $\mu$  with confidence level

$$100(1 - \alpha)\%$$

$\bar{x}$  represents the observed sample mean,  $\sigma$  represents the population standard deviation, and  $n$  represents the sample size.

### Section 7.2

Proposition: If  $n$  is sufficiently large:

$$Z = \frac{\bar{X} - \mu}{S/\sqrt{n}}$$

has approximately a standard normal distribution, with  $\bar{X}$  being the random variable for the sample mean,  $S$  being the random variable for the sample standard deviation.

## A Confidence Interval for a Population Proportion

$p$  : proportion of success in a population

$n$  : sample size

$X$  : # of successes in a sample, a random variable

$x$  : observed # of successes in a sample

$\hat{p} : \frac{x}{n}$

$\hat{q} : 1 - \hat{p}$

Assumptions:

- Population size is larger than  $n$
- $np \geq 10$
- $n(1 - p) \geq 10$

Proposition:

$$\tilde{p} = \frac{\hat{p} + \frac{(z_{\alpha/2})^2}{2n}}{1 + \frac{(z_{\alpha/2})^2}{n}}$$

The confidence interval for a population proportion  $p$  with confidence level  $100(1 - \alpha)\%$  is:

$$\tilde{p} \pm z_{\alpha/2} \frac{\sqrt{\frac{\hat{p}\hat{q}}{n} + \frac{(z_{\alpha/2})^2}{4n^2}}}{1 + \frac{(z_{\alpha/2})^2}{n}}$$

Under certain conditions, the interval is:

$$\tilde{p} \pm z_{\alpha/2} \sqrt{\frac{\hat{p}\hat{q}}{n}}$$

You can find all my notes at <http://omgimanerd.tech/notes>. If you have any questions, comments, or concerns, please contact me at [alvin@omgimanerd.tech](mailto:alvin@omgimanerd.tech)